

Don't Leave These Points on the Table

Probability questions are fundamental, often straightforward, and highly "gettable".

- ✓ **The Opportunity:** While probability helps quantify uncertainty in the real world, on the ACT, it is a known quantity.
- ✓ **The Strategy:** These questions are low-effort, high-reward opportunities. Master the proven strategies to secure these quick points efficiently.

MASTER QUESTIONS
TO GAIN POINTS

2-4

Questions Per Test

+2-3

Points to Composite Score

The Core Logic: Part Over Whole

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$$P(\text{event}) = \frac{\text{Number of favorable outcomes}}{\text{Total number of possible outcomes}}$$

Think: Part / Whole

The Definition:
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Probability measures how likely an event is to occur.

The Memory Trick:
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Think of it simply as fraction logic. The numerator is the 'part' you want. The denominator is the 'whole' of all possibilities.

Key Insight:
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If you can identify what you want and what is possible, you can solve the problem.

The Scale of Certainty

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The Rule: Helvetica Now Display

Probability is always expressed as a number between 0 and 1.

Formats: Helvetica Now Display

Answers can appear as fractions ($1/4$), decimals (0.25), or percentages (25%).

Sanity Check: Helvetica Now Display

If you calculate a number less than 0 or greater than 1, you have made a mistake. Stop and re-evaluate.

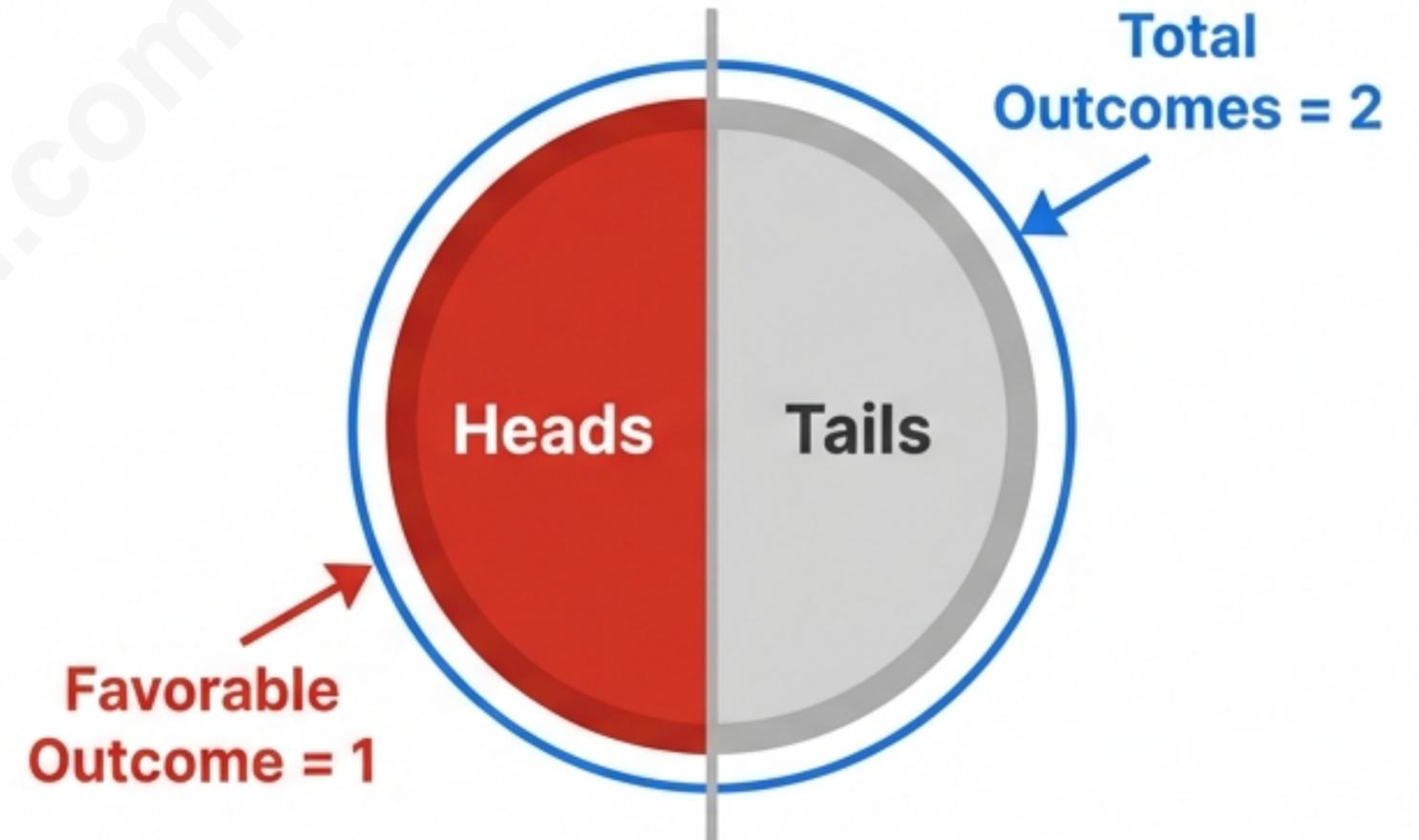
Scenario A: The Coin Flip

The Breakdown

The Problem: What is the probability of flipping a fair coin and getting heads?

- **Step 1 (Total):** A coin has 2 sides.
Total outcomes = 2.
- **Step 2 (Favorable):** We want heads.
Favorable outcomes = 1.
- **Step 3 (Solve):** $P(\text{heads}) = 1/2$.
- **Conversion:** $1/2 = 0.5 = 50\%$.

The Visual



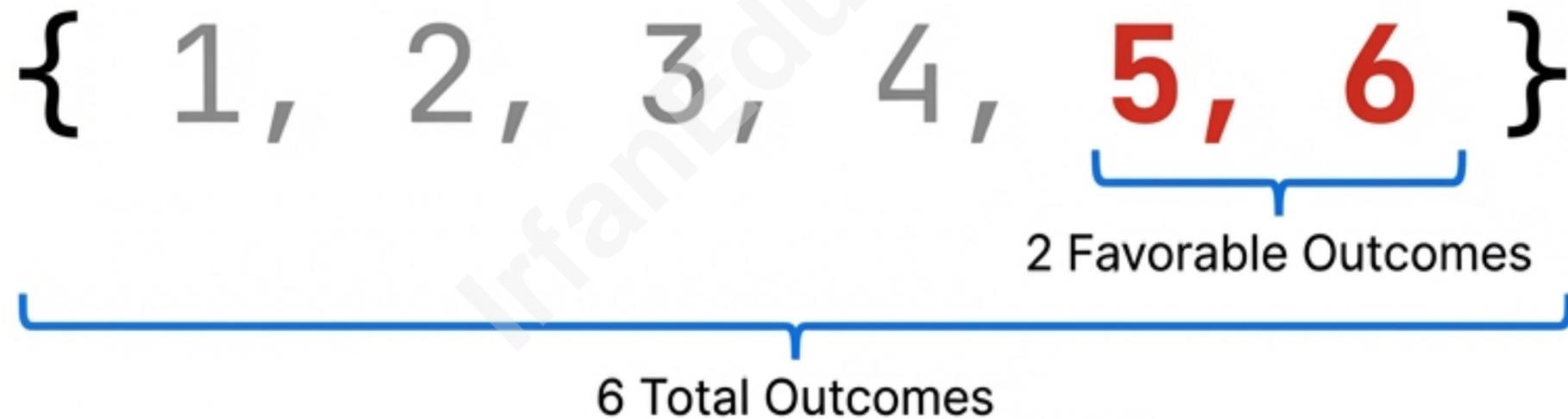
Takeaway: Identify the universal constants first.

Scenario B: The List Strategy

The Problem: What is the probability of rolling a number *greater than 4* on a standard die?

The Trap: Guessing the count.

The Fix: List it out.



$$P = 2/6 = \frac{1}{3}$$

Pro Tip: Writing out the list {5, 6} takes 5 seconds but guarantees accuracy.

The 'Not' Strategy

Complementary Probability

The Breakdown

The Concept: Sometimes it is easier to calculate what you *don't* want and subtract it from 1.

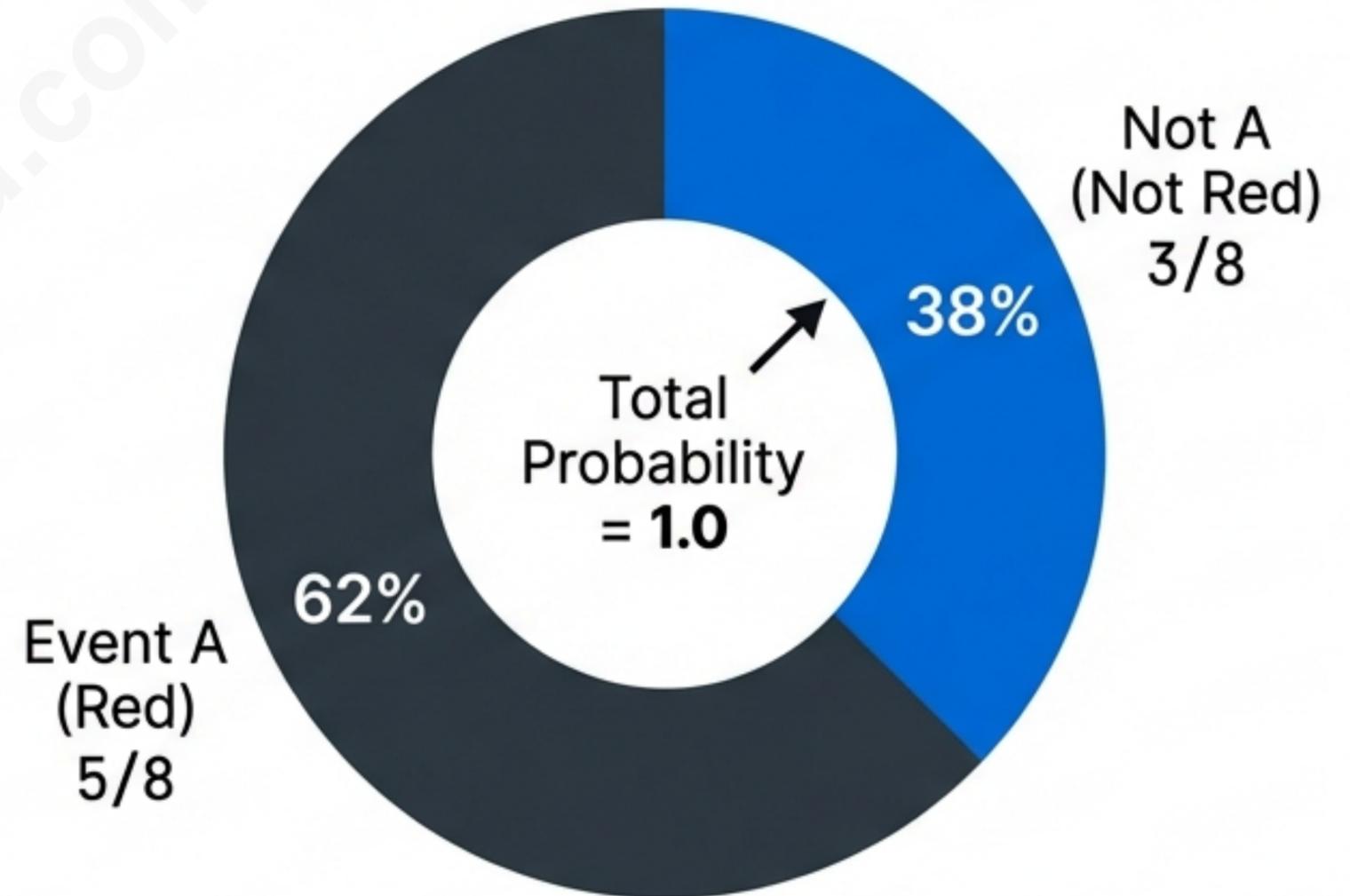
The Formula: $P(\text{not } A) = 1 - P(A)$

Example: If probability of drawing Red is $5/8$, then:

Probability of *Not* Red = $1 - 5/8 = 3/8$.

When to Use: Look for keywords like "Not", "At least one", or "None".

The Visual



Probability is Decision-Making Science



Weather Forecasts.
Meteorologists use probability to predict rain chances (e.g., 70% chance), helping you decide whether to bring an umbrella.



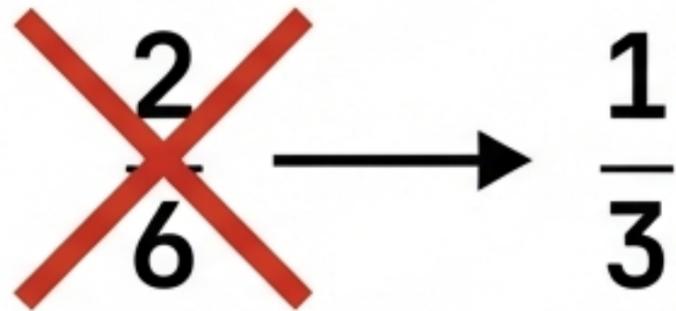
Medical Diagnosis.
Doctors use it to assess risk and treatment success rates. It helps quantify uncertainty.



Finance & Gaming.
Used for risk assessment, market analysis, and balancing game mechanics. It is essential for data literacy.

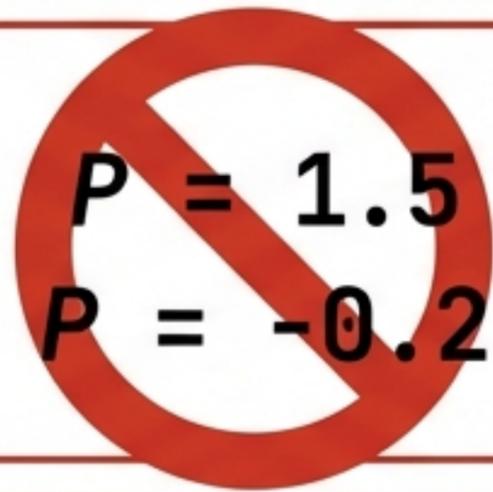
Bottom Line: The ACT tests this because it is the language of modern decision-making.

Avoid These Common ACT Traps


$$\cancel{\frac{2}{6}} \longrightarrow \frac{1}{3}$$

Trap 1: The Unsimplified Fraction

The ACT builds wrong answers based on this. Always reduce terms.


$$\begin{aligned} P &= 1.5 \\ P &= -0.2 \end{aligned}$$

Trap 2: The Impossible Number

Any answer > 1 or < 0 is an immediate red flag. Probability is bounded by 0 and 1.

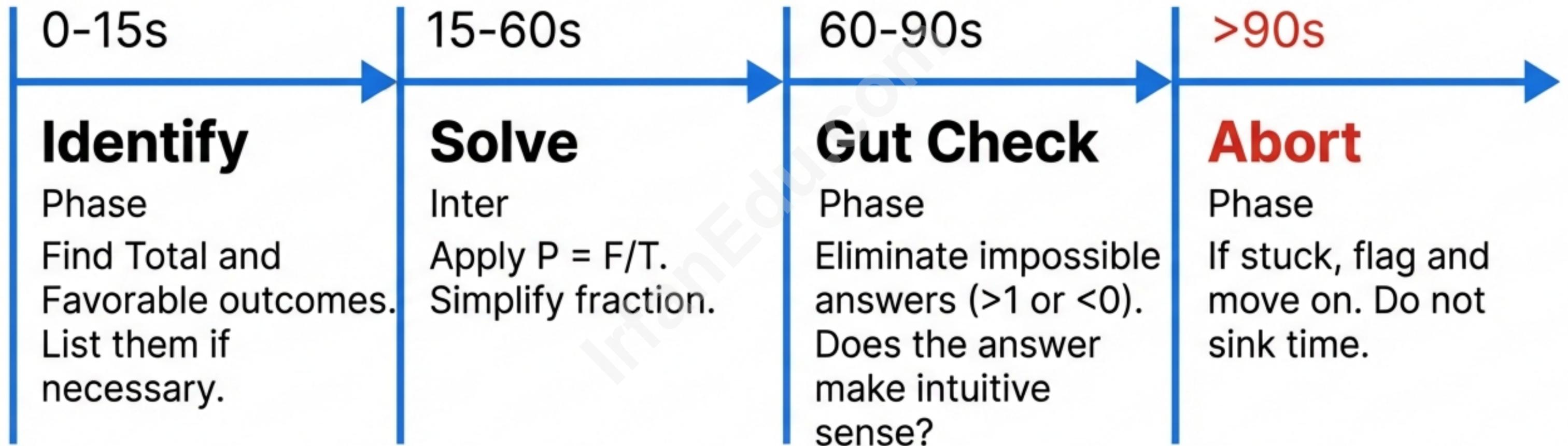


~~Total / Favorable~~
~~Favorable / Total~~ ✓

Trap 3: The Inversion

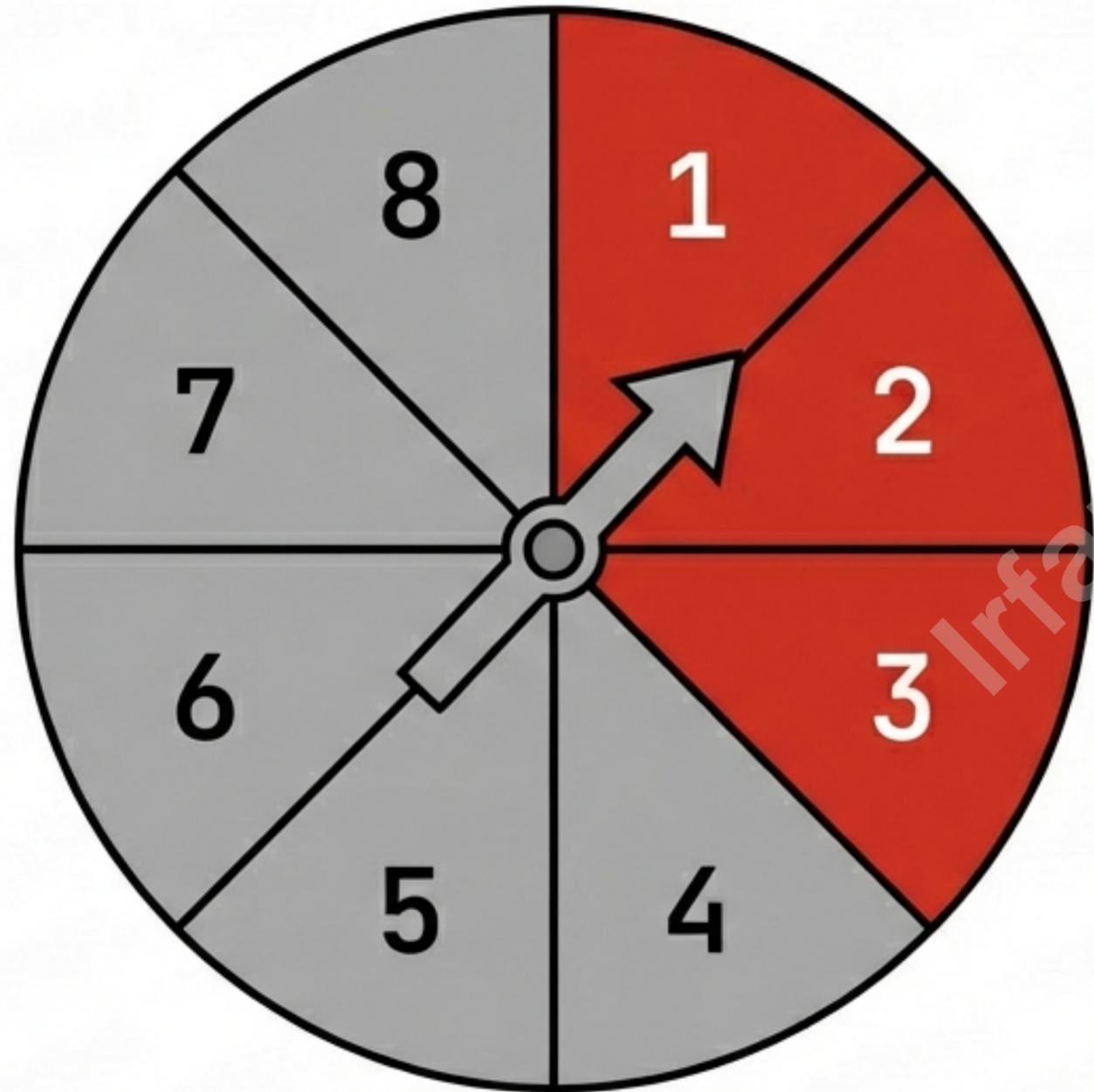
Confusing the numerator and denominator. Remember: It is always Want over Possible.

ACT Test-Taking Protocol



Strategic Guessing: Eliminate impossible answers first. If more than half the outcomes are favorable, the answer must be > 0.5 .

Practice Lab: The Spinner



Question:

What is the probability of spinning a number less than 4?

Analysis:

- Total Sections = 8
- Favorable (Numbers < 4) = {1, 2, 3}.
Count = 3. (Data in JetBrains Mono)

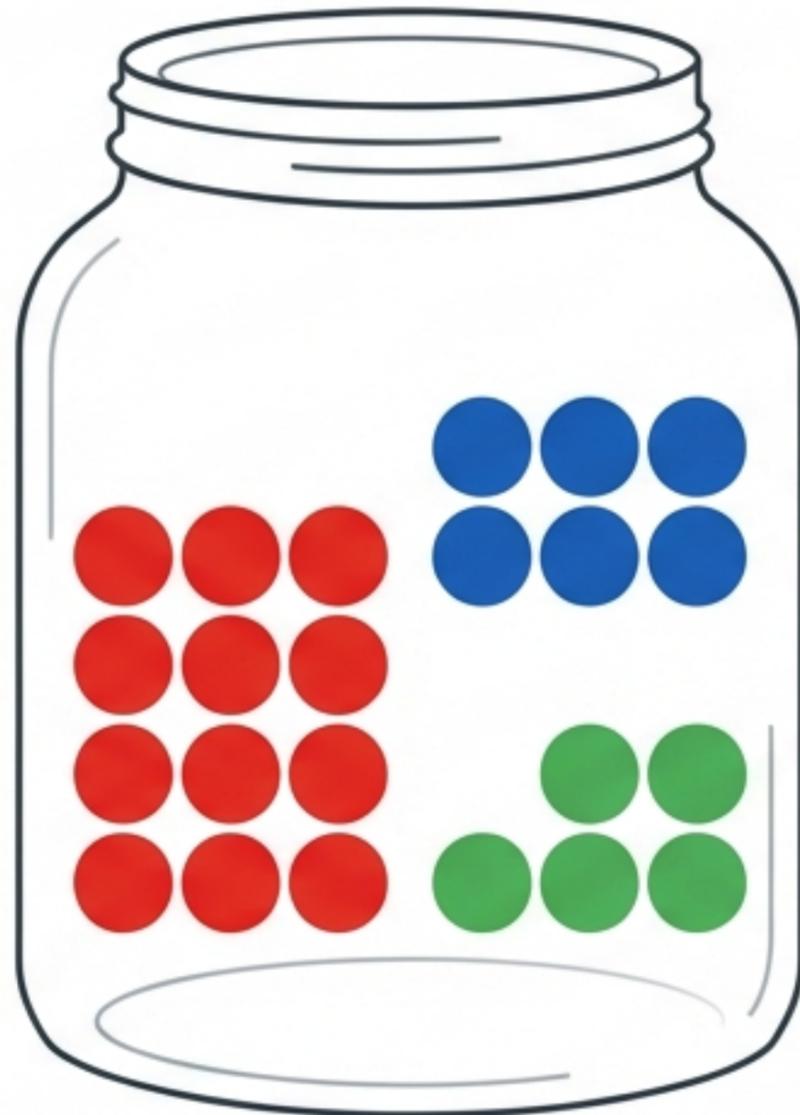
Solution:

$$P = \frac{3}{8}$$

Target Time: 30-40 seconds.

Practice Lab: The Complement

Marbles & The "Not" Rule



Question:

If one ball is selected, what is the probability it is **NOT** blue?

Total: $12 + 8 + 5 = 25$.

Method A (Direct):

Count Red + Green: $12 + 5 = 17$.

$$P = 17/25$$

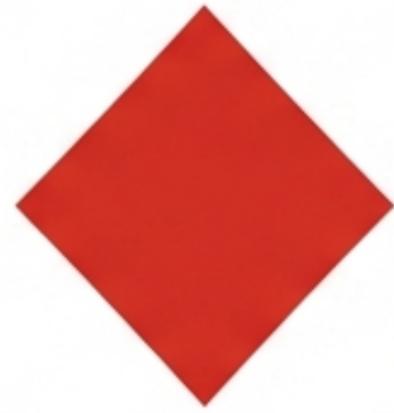
Method B (Complement):

$$P(\text{Blue}) = 8/25$$

$$P(\text{Not Blue}) = 1 - 8/25 = 17/25$$

Strategy: Choose the path of least resistance.

Practice Lab: The Standard Deck



The Facts: A standard deck has 52 cards. There are 4 suits. Each suit has 13 cards.

Memorize: Total = 52. Suit Count = 13.

Question:

What is the probability of randomly drawing a heart?

Analysis:

- Total: 52 cards.
- Favorable: 13 hearts.

Solution:

$$P(\text{heart}) = 13/52 \longrightarrow \mathbf{1/4}$$

Note: Always look for the simplified fraction in the answer choices.

Confidence Comes From Competence

Summary:

You now possess the tools to capture 2-3 extra points on the ACT.

Next Steps:

Solve 10-15 probability problems from official practice tests.

Final Thought:

The more you practice identifying “Favorable” and “Total”, the faster you will become. **Go get those points.**

Related Topics:

Statistics, Ratios, Percentages.

